

# उत्तर प्रदेश राजर्षि टण्डन मुक्त विश्वविद्यालय, प्रयागराज

Bachelor of Science कार्यक्रम अधिन्यास सत्र 2020-21

कोर्स कोड : Course Code: <b>UGMM-101</b>	कोर्स शीर्षक:— (Course Title) <b>Differential Calculus</b>	अधिकतम अंक : 30 <b>Maximum Marks : 30</b>
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खण्ड अ

Section-A

अधिकतम अंक : 18

Maximum Marks : 18

**नोट— (Instructions): Section A consists of long answer questions. Answer should be in 800 to 1000 words. All questions are compulsory.**

1. How many relations can be defined in a set containing 10 elements? If  $A = \{1, 2, 3\}$  then write down the smallest and biggest reflexive relations in the set A.
2. Prove that  $f: X \rightarrow Y$  is injective iff  $f^{-1}(\{y\}) = \{x\} \forall y \in f(X)$ , and some  $x \in X$
3. If  $\lim_{x \rightarrow a} f(x) = l$  then show that  $\lim_{x \rightarrow a} |f(x)| = |l|$   
(Hint: Use  $||f(x) - l| \geq ||f(x)| - |l||$ )

खण्ड ब

Section -B

अधिकतम अंक : 12

Maximum Mark : 12

**नोट— (Instructions): Section B consists of short answer questions. Answer should be in 200 to 300 words. All questions are compulsory.**

4. Show that  $\lim_{x \rightarrow 0} \frac{e^x - e^{-x}}{e^x + e^{-x}}$  does not exist.
5. Find  $\frac{dy}{dx}$  if  $x = a \cos^3 t$ ,  $y = a \sin^3 t$
6. Expand  $\log(x + a)$  in powers of  $x$  by Taylor's theorem.
7. Verify Lagrange's formula for the function  $f(x) = 2x - x^2$  on  $[0,1]$ .

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Bachelor of Science कार्यक्रम अधिन्यास सत्र 2020-21

कोर्स कोड : Course Code: <b>UGMM-102</b>	कोर्स शीर्षक:- (Course Title) <b>Analytical Geometry</b>	अधिकतम अंक : 30 <b>Maximum Marks : 30</b>
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खण्ड अ

Section-A

अधिकतम अंक : 18

Maximum Marks : 18

**नोट— (Instructions): Section A consists of long answer questions. Answer should be in 800 to 1000 words. All questions are compulsory.**

1. Show that the equation  $12x^2 - 10xy + 2y^2 + 11x - 5y + 2 = 0$  represents a pair of straight lines. Find their equations.
2. Find the coordinates of the centre of the conic  $41x^2 + 24xy + 9y^2 - 130ax - 60ay + 116a^2 = 0$ .
3. The coordinates of a point  $A$  are  $(2, 3, -5)$ . Determine the equation to the plane through  $A$  at right angles to the line  $OA$ , where  $O$  is the origin.

खण्ड ब

Section -B

अधिकतम अंक : 12

Maximum Mark : 12

**नोट— (Instructions): Section B consists of short answer questions. Answer should be in 200 to 300 words. All questions are compulsory.**

4. Find the equation of the sphere which passes through the points  $(0,0,0)$ ,  $(a, 0,0)$ ,  $(0, b, 0)$  and whose centre lies on the plane  $x + y + z = 0$
5. Find the equation of the cylinder with generators parallel to the  $x$ -axis and passing through the circle  $x^2 + y^2 + z^2 = 9$ ,  $2x = y + z$ .
6. Find the equation of the cone reciprocal to the cone  
 $fyz + gzx + hxy = 0$
7. Show that the plane  $7x + 5y + 3z = 30$  touches the ellipsoid  $7x^2 + 5y^2 + 3z^2 = 60$ . Find the point of contact.

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Bachelor of Science कार्यक्रम अधिन्यास सत्र 2020-21

कोर्स कोड : Course Code: <b>UGMM-103</b>	कोर्स शीर्षक:— (Course Title) <b>Integral Calculus</b>	अधिकतम अंक : 30 <b>Maximum Marks : 30</b>
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खण्ड अ

Section-A

अधिकतम अंक : 18

Maximum Marks : 18

**नोट— (Instructions): Section A consists of long answer questions. Answer should be in 800 to 1000 words. All questions are compulsory.**

1. Evaluate the following integrals

(a)  $\int a^{2x} \cos 4x \, dx$  (b)  $\int e^{3x} \sin 3x \, dx$  (c)  $\int e^{4x} \cos x \cos 2x \, dx$

2. Prove : If  $C_n = \int e^{ax} \cos^n x \, dx$ , then

$$C_n = \frac{ae^{ax} \cos^n x}{n^2 + a^2} + \frac{ne^{ax} \cos^{n-1} x \sin x}{n^2 + a^2} + \frac{n(n-1)}{n^2 + a^2} C_{n-2}$$

3. Evaluate  $\int \frac{x^2 + 2x + 3}{\sqrt{x^2 + x + 1}}$

खण्ड ब

Section -B

अधिकतम अंक : 12

Maximum Mark : 12

**नोट— (Instructions): Section B consists of short answer questions. Answer should be in 200 to 300 words. All questions are compulsory.**

4. Prove that the line  $2x + 3y = 1$  touches the curve  $3y = e^{-2x}$  at a point whose X-coordinate is zero.

5. Show that the curve  $x^3 + 2x^2 + 2xy - y^2 + 5x - 2y = 0$

has a single cusp & first species at the point  $(-1, -2)$

6. Find the area of the curve  $x = a(3 \sin \theta - \sin^3 \theta)$ ,  $y = a \cos^3 \theta$ ,  $0 \leq \theta \leq 2\pi$ .

7. Find the area of the surface generated by revolving the circle  $r = a$  about the x-axis thus verify that the surface area of a sphere of radius a is  $4\pi a^2$ .

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Bachelor of Science कार्यक्रम अधिन्यास सत्र 2020-21

कोर्स कोड : Course Code: <b>UGMM-104</b>	कोर्स शीर्षक:— (Course Title) <b>Differential Equation</b>	अधिकतम अंक : 30 <b>Maximum Marks : 30</b>
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खण्ड अ

Section-A

अधिकतम अंक : 18

Maximum Marks : 18

**नोट— (Instructions): Section A consists of long answer questions. Answer should be in 800 to 1000 words. All questions are compulsory.**

1. Verify that the function  $y = a \cos x + b \sin x$ , where  $a, b \in \mathbb{R}$  is a solution of the differential equation  $\frac{d^2 y}{dx^2} + y = 0$ .
2. Show that the differential equation  $\frac{dy}{dx} = \frac{x^2 + y^2}{x^2 + xy}$  is homogeneous and solve it.
3. Solve the equation  $x \frac{dy}{dx} = x^2 + 3y$ ,  $x > 0$ .

खण्ड ब

Section –B

अधिकतम अंक : 12

Maximum Mark : 12

**नोट— (Instructions): Section B consists of short answer questions. Answer should be in 200 to 300 words. All questions are compulsory.**

4. Solve the differential equation  $x dy + y dx = \frac{a^2 (x dy - y dx)}{x^2 + y^2}$ .
5. Solve the differential equation  $y = x + a \tan^{-1} p$
6. Determine the curve whose sub-tangent is twice the abscissa of the point of contact and passes through the point (1, 2).
7. With reference to the following figure, which consists of a resistor of resistance  $R = 3 \Omega$ , connected in series with an inductor of inductance  $L = 5 \text{ H}$ , and an applied constant voltage  $E = 240 \text{ Volts}$ .
  - (i) Obtain a differential equation giving the current  $I$  at time  $t$ .
  - (ii) Solve the differential equation for the initial condition, when  $t = 0, I = 0$ .