

**UGMM-01**  
**Calculus**

**Block-I      Real Numbers and Functions**

- Unit-01      Limit and Continuity
- Unit-02      Differentiation
- Unit-03      Derivatives of Trigonometric Functions
- Unit-04      Derivatives of Some Standard Functions exponential functions logarithmic functions, hyperbolic functions

**Block-II      Drawing Curves**

- Unit-05      Higher Order Derivatives 2<sup>nd</sup> & 3<sup>rd</sup> & 4<sup>th</sup> Order derivatives, Leibniz theorem, Taylor's theorem and Maclaurin's Series
- Unit-06      The UPS and Downs- Maxima and Minima of the Functions, Mean Value Theorems, Rolle's th & Lagrange's th, Sufficient Conditions for the Existence of extreme Points, Convexity and Concavity, Points of Inflections
- Unit-07      Geometrical Properties of Curves- Tangent and Normals, Angle of Intersection, Asymptotes
- Unit-08      Curve Tracing- Cartesian Eq<sup>n</sup>, Polar Eq<sup>n</sup>, and Cartesian Eq<sup>n</sup>

**Block-III      Integral Calculus**

- Unit-09      Definite Integral
- Unit-10      Methods of Integration
- Unit-11      Reduction Formulas
- Unit-12      Integration of Rational and Irrational Function

**Block-IV      Application of Calculus**

- Unit-13      Application of Differential Calculus- Monotonic function, Approximate Values, Inequalities
- Unit-14      Area under a Curve- Cartesian eq<sup>n</sup> Polar Eq<sup>n</sup> Area bounded by a closed curve, Trapezoidal rule, Simpson's rule
- Unit-15      Application of Integral Calculus- Length of plane curve, Cartesian form, Parametric form, polar form, Volume of Solid of Revolution, area of Surface of Revolution

## UGMM-02

### Linear Algebra

<b>Block-I</b>	<b>Vector Space</b>
Unit-01	Sets, Functions and Fields
Unit-02	Two and Three Dimensional Spaces
Unit-03	Vector Space
Unit-04	Basis and Dimension
<b>Block-II</b>	<b>Linear Transformation and Matrices</b>
Unit-05	Linear Transformation-I- Range Space and the Kernel, Rank and Nullify Homomorphism Th
Unit-06	Linear Transformation-II- Vector Space of Matrices, Transpose, Conjugate, Conjugate, Transpose, Diagonal Matrix, Triangular Matrix, Multiplication Inverlible Matrix
Unit-07	Matrices-I- Vector Space of Matrices, Transpose, Conjugate, Conjugate Transpose, Diagonal Matrix, Triangular Matrix, Multiplication Inverlible Matrix
Unit-08	Matrices-II- Rank of Matrix, Elementary Operations, and its Applications
<b>Block-III</b>	<b>Eigen Values and Eigenvectors</b>
Unit-09	Determinants
Unit-10	Characteristics and Minimal Polynomials- Cayley Hamilton Theorem, Minimal polynomial
<b>Block-IV</b>	<b>Inner Production and Quadratic Forms</b>
Unit-11	Inner Production Spaces
Unit-12	Hermitian Unitary Operators
Unit-13	Real Quadratic Forms
Unit-14	Conies

## UGMM-03

### Mathematical Methods

#### **Block-I Algebra and Geometry**

- Unit-01 Sets and Functions
- Unit-02 Graphs and Functions
- Unit-03 Elementary Algebra
- Unit-04 Coordinate Geometry
- Unit-05 Vectors

#### **Block-II Calculus**

- Unit-06 Differential Calculus
- Unit-07 Applications of Differential Calculus
- Unit-08 The Integration
- Unit-09 Integration of Elementary Functions
- Unit-10 Differential Equations

#### **Block-III Probability Distribution**

- Unit-11 Statistics- Random Variables, Sampling, Frequency Distribution of data, Measure of Central Tendency, Mean, Median, Mode, Measures of Dispersion
- Unit-12 Probability
- Unit-13 Discrete Probability Distribution- Binomial Distribution, Poisson Distribution
- Unit-14 Continuous Probability Distribution- Uniform Distribution, Exponential Distribution, Normal Distribution

#### **Block-V Statistical Inference**

- Unit-15 Statistical data Sampling- Sample Selection, Sampling Distribution, Standard Error, Unbiased Estimator, Precision and Accuracy of the Sample Estimator, Types of Sample Design, Stratified Random Sampling, Cluster Sampling
- Unit-16 Hypothesis Tests- Level of Significance, Degrees of Freedom, Chi-Square Test, t-test, ANOVA
- Unit-17 Correlation and Regression

## UGMM-04

### Elementary Algebra

<b>Block-I</b>	<b>Solutions of Polynomial Equations</b>
Unit-01	Sets
Unit-02	Complex Number- Geometrical Representations, Algebraic Operations, De-moivre's Theorem
Unit-03	Cubic and Biquadrate Equations
<b>Block-II</b>	<b>Equations and Inequalities</b>
Unit-04	Systems of Linear Equations
Unit-05	Cramer's Rule
Unit-06	Inequalities

## UGMM-05

### Analytical Geometry

<b>Block-I</b>	<b>Conies</b>
Unit-01	Preliminaries in Plane Geometry
Unit-02	Standard Conies- Parabola, Ellips, Hyperbola, Polar Equations of Conies
Unit-03	General Theory of Conies- 2 <sup>nd</sup> Degree Equation, Central and Non- Central Conies, Tracing a Conic, Tangents, Intersection of Conies
<b>Block-II</b>	<b>Sphere, Cone and Cylinder</b>
Unit-04	Preliminaries in 3Dimensional Geometry- Points, Lines, Planes
Unit-05	The Sphere- Equations of Sphere, Tangent Lines and Plans, Lines Planes, Intersection of Spheres
Unit-06	Cones and Cylinder
<b>Block-III</b>	<b>Conicoids</b>
Unit-07	General Theory of Conicoids
Unit-08	Central Conicoids
Unit-09	Paraboloids

## UGMM-06

### Abstract Algebra

<b>Block-I</b>	<b>Elementary Group Theory</b>
Unit-01	Sets and Functions
Unit-02	Groups
Unit-03	Subgroups
Unit-04	Lagrange's Theorem
<b>Block-II</b>	<b>Some More Group Theory</b>
Unit-05	Normal Subgroups
Unit-06	Group Homomorphisms
Unit-07	Permutation Groups
Unit-08	Finite Group
<b>Block-III</b>	<b>Elementary ring Theory</b>
Unit-09	Rings
Unit-10	Sub Rings and Ideals
Unit-11	Ring Homomorphisms
<b>Block-IV</b>	<b>Integral Domains and Fields</b>
Unit-12	The Basics
Unit-13	Polynomial Rings
Unit-14	Special Integral Domains
Unit-15	Irreducibility and Field Extensions

## UGMM-07

### Advanced Calculus

<b>Block-I</b>	<b><math>R^\infty</math> and <math>R^n</math></b>
Unit-01	Infinite Limits
Unit-02	L-Hospital's Rule
Unit-03	Functions of Several Variables
<b>Block-II</b>	<b>Partial Derivatives</b>
Unit-04	Limits and Continuity
Unit-05	First Order Partial Derivatives and Differentiability
Unit-06	Higher Order Partial Derivatives
Unit-07	Chain Rule and Directional Derivatives
<b>Block-III</b>	<b>Applications of Partial Derivatives</b>
Unit-08	Taylor's Theorem
Unit-09	Jacobians
Unit-10	Implicit and Inverse Function Theorems
<b>Block-IV</b>	<b>Multiple Integrations</b>
Unit-11	Double Integration
Unit-12	Triple Integration
Unit-13	Applications of Integrals
Unit-14	Line Integrals in $R^2$

**UGMM-08**  
**Differential Equations**

<b>Block-I</b>	<b>Ordinary Differential Equations of First Order</b>
Unit-01	The Nature of Differential Equations
Unit-02	Methods of Solving First Order and First Degree Equations
Unit-03	Linear Differential Equations
Unit-04	Differential Equations of First Order but not of First Degree
<b>Block-II</b>	<b>Second and Higher Order Ordinary</b>
Unit-05	Nigher Order Linear Differential Equations
Unit-06	Method of Unditermined Coefficients
Unit-07	Method of Variation of Parameters
Unit-08	Method of Symbolic Operators
Unit-09	Second Order Linear Differential Equations
<b>Block-III</b>	<b>First Order Partial Differential Equations</b>
Unit-10	Curves and Surfaces
Unit-11	Simultaneous Differential Equations
Unit-12	Pfaffian Differential Equations
Unit-13	Linear Partial Differential Equations
Unit-14	Non-Linear Partial Differential Equations
<b>Block-IV</b>	<b>Second and Higher Order Partial Differential Equations</b>
Unit-15	Homogeneous Linear partial Differential Equations with Constant Coefficients
Unit-16	Non- Homogeneous Linear partial Differential Equations with Constant Coefficients
Unit-17	Partial Differential Equations of Second Order

## UGMM-09

### Real Analysis

#### **Block-I Real numbers and Functions**

- Unit-01 Sets and Numbers
- Unit-02 Structure of Real Numbers
- Unit-03 Topology of the Real Line
- Unit-04 Real Functions

#### **Block-II Sequences and Series**

- Unit-05 Sequences- Bounded Monotonic, Convergent, Cauchy
- Unit-06 Positive Term Series
- Unit-07 General Series- Comparison Tests, P-Test, d' Alembert's Ratio test, Raabe's Test, Gauss's Test, Leibnitz's Series, Absolute and Conditional Convergence

#### **Block-III Limit and Continuity**

- Unit-08 Limit of a Function
- Unit-09 Continuity
- Unit-10 Properties of Continuous Functions- Continuity on Bounded Closed Intervals, Point wise Continuity and Uniform Continuity

#### **Block-IV Differentiability**

- Unit-11 Derivatives
- Unit-12 Mean Value Theorems- Roll's Theorem, Lagrange's Theorem, Cauchy's Mean Value theorem, Generalised mean Value Theorem Darboux Theorem
- Unit-13 Higher Order Derivatives- Taylor's Theorem, Maclaurin's Expansion
- Unit-14 Integrability
- Unit-15 The Riemann Integration
- Unit-16 Integrability and Differentiability
- Unit-17 Sequences and Series of Functions- Convergence Point Convergence, Uniform



## UGMM-10

### Numerical Analysis

<b>Block-I</b>	<b>Solutions of Non-Linear Equations in one Variable</b>
Unit-01	Review of Calculus- Intermediate Value Theorem Roll's Theorem Lagrange's Mean Value Theorem, Taylor's Theorem, Round off Error Truncation Error
Unit-02	Iteration Methods for Finding Roots- Initial Approximation to a Root, Bissction Method, Fixed Point Iteration Method
Unit-03	Chord Methods for Finding Roots- Regula Falsi Method, Newton Raphson Method, Convergence Criterion
Unit-04	Approximate Roots of Polynomial Equations- Birge Vieta Method Graeffe's Root Squaring Method
<b>Block-II</b>	<b>Solutions of Linear Algebraic Equations</b>
Unit-05	Direct Methods- Proliminaries Cramer's Rule, Gauss, Elimination Method, LU Decomposition Method
Unit-06	Inverse of Square :Matrix- Method of Adjoints, The Gaurs- Jordon Reduction Method, LU Decomposition Method
Unit-07	Iterative Method- General Iteratia Method, Jacobi Iteration Method, The Gauss-Seidel Iteration Method
Unit-08	Eigen Values and Eigen Vectors- The Eigen Value Problem, the Power Method, The Inverse power method
<b>Block-IV</b>	<b>Interpolation</b>
Unit-09	Lagrange's Form
Unit-10	Newton Form of the Interpolating Polynomial
Unit-11	Interpolation at Equally Spaced Points- Forward and Back ward Differences, Newton's Forward and Backward Difference Formula
<b>Block-V</b>	<b>Numerical Differentiation, Integration and Solutions of Differentiation Equations</b>
Unit-12	Numerical Differentiation
Unit-13	Numerical Integration
Unit-14	Numerical Solutions of Ordinary Differential Equations- Taylor Series Method, Euler's Method, Richardson's Extrapolation
Unit-15	Numerical Solutions of Numerical Equations Using runge- Kutta Methods- 2 <sup>nd</sup> , 3 <sup>rd</sup> , and 4 <sup>th</sup> Order.

## UGMM-11

### Probability and Statistics

#### **Block-I Descriptive Statistics**

- Unit-01 Frequency Distribution of a Character
- Unit-02 Measure of Central Tendency and Dispersion
- Unit-03 Skewness and Kurtosis
- Unit-04 Correlation and Regression

#### **Block-02 Probability on Discrete Sample Spaces**

- Unit-05 Sample Space of a Random Experiment
- Unit-06 Probability on a Discrete Sample
- Unit-07 Discrete Random Variable and its Probability Distribution- Random Variable, Joint and Marginal Distribution and its independence, Mathematical Expectation, Moments and Moments Generating Functions, Covariance
- Unit-08 Standard Probability Distribution-I- Bernaulli Distribution, Binomial Distribution, Hyper geometric Distribution
- Unit-09 Standard Probability Distribution-II- Geometric Distribution, Negative Binomial Distribution, Poisson Distribution.

#### **Block-III Distribution Theory**

- Unit-10 Univariable Distributions- Distribution Functions, Density Functions, Expectation and Variance, Momeats and Moments Generating Functions.
- Unit-11 Standard Continues Distributions- Normal Distribution, Exponential and Gamma Distribution, Beta Distribution.
- Unit-12 Bivariate Distribution- Density Functions, Distribution Functions, Conditional Distribution, Independnee Expectations, Correlation and Regression.
- Unit-13 Functions Random Variables- Direct Approach Transformation Approach, Chi-Squala Distribution, Independnee Expectations, Correlation and Regression
- Unit-14 Limit Theorms- Chebyshev's Inequality, Weak Law of Large Numbers, Poisson Approximation to Binomial, Central Limit Theorem.

#### **Block-IV Elements of Statistical Inference**

- Unit-15 General Introduction- Inductive Inference, Random Sampling, Sampling Distributions, Related to Normal Distribution, Point Extimation Testing of Hypothesis, Interval Estimation

- Unit-16 Point Estimation- Properties of Estimators, Method of Moments, Method of Maximum Likelihood.
- Unit-17 Testing of Hypotheses- Some Concepts, Neyman- Pearson Lemma, Likelihood-Ratio Tests
- Unit-18 Common Tests and Confidence Intervals- Some Common Tests of Hypothesis for Normal Populations, Confidence Intervals, Chi- Square test for Goodness of Fit.

## UGMM-12

### Linear Programming

<b>Block-I</b>	<b>Basic Mathematics and Optimization</b>
Unit-01	Basic Algebra- Matrices and Determinants, Vector
Unit-02	Inequalities and Convex Sets
Unit-03	Optimization in two Variables
Unit-04	Optimization in More Than Two Variables
<b>Block-II</b>	<b>Simplex Method and Duality</b>
Unit-05	Standard Form and Solutions
Unit-06	Simplex Method
Unit-07	Primal and Dual
Unit-08	Duality Theorems
<b>Block-III</b>	<b>Special Linear Programming Problems</b>
Unit-09	Transportation Problem
Unit-10	Feasible Solution of the Transportation
Unit-11	The Assignment Problem
<b>Block-IV</b>	<b>Game Theory</b>
Unit-12	Games With Pure Strategies
Unit-13	Games With Mixed Strategies
Unit-14	Graphical Method and Dominance
Unit-15	Games and Linear Programming

## UGMM-13

### Discrete Mathematics

<b>Block-I</b>	<b>Elementary Logic</b>
Unit-01	Propositional Calculus- Propositions, Logical Connectives, Logical Equivalence, Logical Quantifiers
Unit-02	Methods of Proof- Direct Proof, Indirect Proof, Counterexamples, Principle of Induction
Unit-03	Boolean Algebra and Circuits- Boolean Algebra, Boolean Expressions, Logic Circuits Boolean Functions
<b>Block-II</b>	<b>Basic Combinatorics</b>
Unit-04	Combinatorics An Introduction- Multiplications and Addition Principles, Permutations, Combinations, Binomial Expansion, Multinomial Expansion
Unit-05	Partitions and Distributions
Unit-06	More About Counting- Pigeon Hole Principle, Inclusion Exclusion Principle, Application to Number Theory, Application to Onto Maps, Application to Probability, Applications to Derangements
<b>Block-III</b>	<b>Recurrences</b>
Unit-07	Recurrences Relations
Unit-08	Generating Functions- Exponential, Generating Functions, Linear Equations, Combinatorial Identities
Unit-09	Solving Recurrences- Linear Homogeneous Recurrences, Linear Non Homogeneous Recurrences, Method of Inspection Method of Telescoping Sum, Method of Iteration, Method of Substitution
<b>Block-V</b>	<b>Graph Theory</b>
Unit-10	Basic Properties of Graphs
Unit-11	Special Graphs- Connected Graphs, Bipartite Graph, Trees
Unit-12	Eulerian and Hamiltonian Graphs- Eulerian Graphs Fleury's Algorithm, Hamiltonian Graphs, Travelling Salesperson Problem
Unit-13	Graph Colorings and Planar Graphs- Vertex Colorings, Planar Graphs, Map Coloring Problem, Edge Colorings.

## UGMM-14

### Mathematical Modeling

#### **Block-I Introduction to Mathematical Modeling**

Unit-01 Mathematical Modeling- An Overview

Unit-02 Formulating A Model

Unit-03 Solving and Interpreting a Model

#### **Block-II Mathematical Modeling in the Physical Environment**

Unit-05 Motion in a Straight Line- Free Fall of a Body, Upward Motion Under Gravity, Simple Harmonic Motion, Projectile Motion.

Unit-06 Planetary Motion- Newton's Law of Gravitation, Particle projected from the Earth, Central Forces, Modeling planetary Motion, Kepler's Law Lead to Newton's Law of Gravitation, Limitations

Unit-07 Air Pollutions- Physical Process, Mathematical Model of Plane Rise, Gaussian Model of Dispersion

#### **Block-III Mathematical Modeling in the Biological Environment**

Unit-08 Blood Flow and Oxygen Transfer

Unit-09 Single Species Population Models

Unit-10 Two Species Population Models

Unit-11 Epidemics

#### **Block-IV Mathematical Modeling in Socio-Economic Environment**

Unit-12 Some Models in Economics- Utility and Demand Function, Production Function and Cost Function, Supply Function, Market Equilibrium, Monopoly, Duopoly and Oligopoly

Unit-13 Conflict and Cooperation- Some Games and its Applications, Two person and Zero-person Game, Co-operative and In-Co-Operative game Theory

Unit-14 Investments- Markowitz Model, Return Valuations, Risk Valuations, Diversifications, Portfolio Selection \

Unit-15 Probabilistic Models- Queuing Models, Queuing Theory Time Series Analysis, Forecasting Models.